

# HarmonicPlanetary® HPGP High Torque Series

## Size

11, 14, 20, 32, 50, 65

6  
Sizes

## Peak Torque

12Nm – 3940Nm

## Reduction Ratio

Single Stage: 3:1 to 9:1, Two Stage: 11:1 to 50:1

## Low Backlash

Standard: <3 arc-min Optional: <1 arc-min

### Low Backlash for Life

Innovative ring gear automatically adjusts for backlash, ensuring consistent, low backlash for the life of the gearhead. The ring gear design automatically provides the optimum backlash in the planetary gear train and maintains the same low backlash for the life of the gearhead.

## High Efficiency

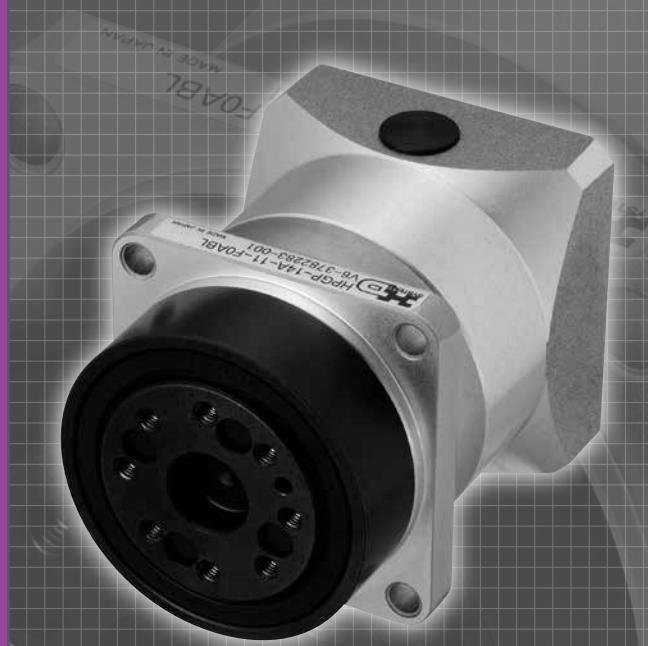
Up to 95%

## High Load Capacity Output Bearing

A Cross Roller bearing is integrated with the output flange to provide high moment stiffness, high load capacity and precise positioning accuracy.

## Easy mounting to a wide variety of servomotors

Quick Connect™ coupling



# CONTENTS

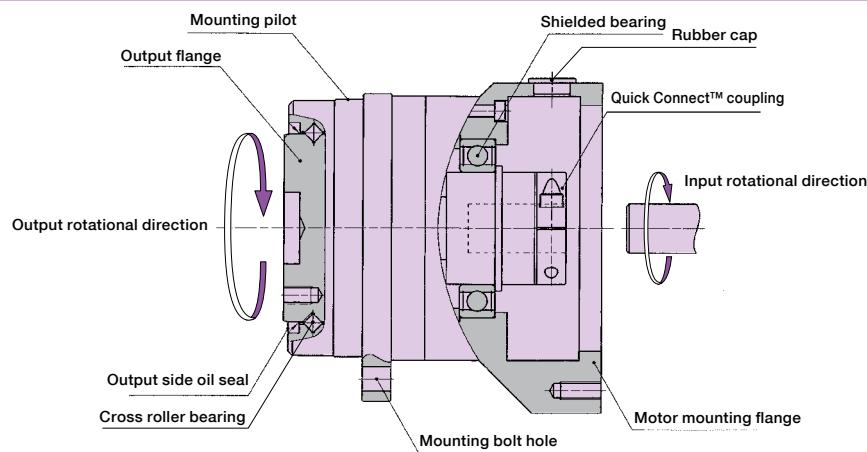
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**HPGP - 11 A - 05 - BL3 - D - F0 - Motor Model Number**

Model Name	Size	Design Revision	Reduction Ratio	Backlash	Input Side Bearing	Output Configuration	Input Configuration & Options
Harmonic Planetary® <b>HPGP</b> High Torque	11	A	5, 21, 37, 45	BL1: Backlash less than 1 arc-min (Sizes 14 to 65)	D: Input side contact sealed bearing (DDU)	F0: Flange output J20: Straight shaft (without key) J60: Straight shaft (with key and center tapped hole)	This code represents the motor mounting configuration. Please contact us for a unique part number based on the motor you are using.
	14		5, 11, 15, 21, 33, 45	BL3: Backlash less than 3 arc-min	Z: Input side bearing with double non-contact shields	F0: Flange output J2: Straight shaft (without key) J6: Straight shaft (with key and center tapped hole) (J2, J6 for Size 65 is also available)	
	20		4, 5, 12, 15, 20, 25				
	32						
	50						
	65						

## Gearhead Construction

Figure 018-1



## Rating Table

Table 019-1

Size	Ratio	Rated Torque <sup>*1</sup>	Limit for Repeated Peak Torque <sup>*2</sup>	Limit for Momentary Torque <sup>*3</sup>	Max. Average Input Speed <sup>*4</sup>	Max. Input Speed <sup>*5</sup>	Mass <sup>*6</sup>					
		Nm	Nm	Nm	rpm	rpm	Shaft	Flange				
11	5	6.6	12	13	20	3000	10000	0.18				
	21	10	0.14									
	37	12	0.24									
	45	13	0.20									
14	5	15	39	39	56	3000	6000	0.54				
	11	20	38					0.42				
	15	21										
	21	23										
	33	27										
20	45	29	0.51									
	5	50		133	142	217	3000	6000				
	11	59		156								
	15	70										
	21	78										
	33	72		156								
32	45	98		142								
	5	150	400	400	650	3000	6000	4.4				
	11	160	440					3.0				
	15	220										
	21	240										
	33	200	440									
50	45	280	400									
	5	380	1460	1850	2180	2000	4500	13				
	11	450						10				
	15	460	1500									
	21	490	1460					12				
	33	620										
65	45	640	1360									
	4	1150	3520	4500	4500	2000	2500	32 <sup>7</sup>				
	5	1190	3790					22				
	12	1350	47 <sup>7</sup>									
	15	1670						3940				
	20	1520						3790				
	25	1900						3840				

<sup>\*1</sup>: Rated torque is based on L<sub>50</sub> life of 20,000 hours at rated input speed.

<sup>\*2</sup>: The limit for torque during start and stop cycles.

<sup>\*3</sup>: The limit for torque during emergency stops or from external shock loads. Always operate below this value. Calculate the number of permissible events to ensure it meets required operating conditions.

<sup>\*4</sup>: Maximum average input speed is limited by heat generation in the speed reducer assuming a continuous operating speed or the average input speed of a motion profile. The actual limit for average input speed depends on the operating environment.

<sup>\*5</sup>: Maximum instantaneous input speed.

<sup>\*6</sup>: The mass is for the gearhead only (without input shaft coupling & motor flange). Please contact us for the mass of your specific configuration.

<sup>\*7</sup>: Flange output is standard for the size 65 gearhead. Shaft type (J2 & J6) is also available.

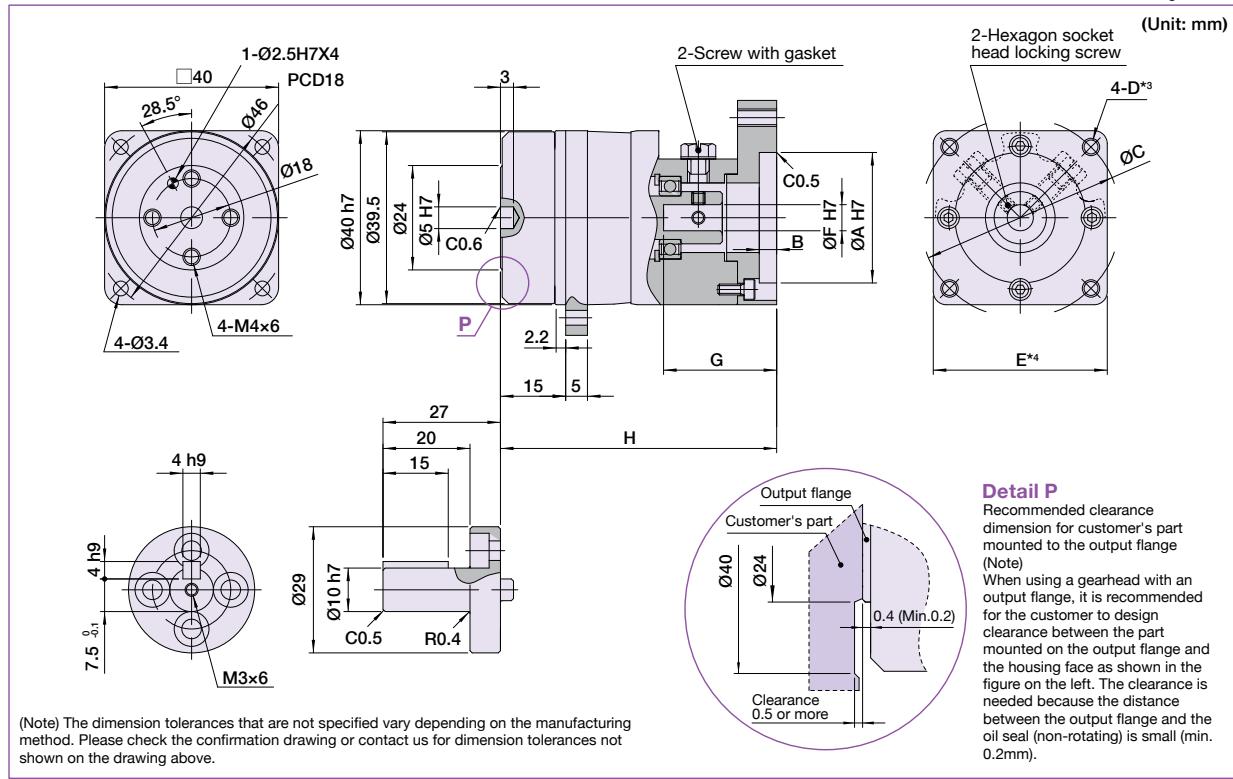




## HPGP-11 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

Figure 022-1



## Dimension Table

(Unit: mm) Table 022-1

	Flange	Coupling	A (H7)		B	C		F (H7)		G		H *1	Mass (kg) *2
			Min.	Max.		Max.	Min.	Max.	Min.	Max.	Min.		
Single Stage	Type I	1	20	50	4	28	70	5	8	17.5	26	54.5	0.34
Two Stage	Type I	1	20	50	4	28	70	5	8	17.5	26	63.5	0.40

Refer to the confirmation drawing for detailed dimensions. Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

\*4 E dimension is dependent on motor selection.

## Moment of Inertia

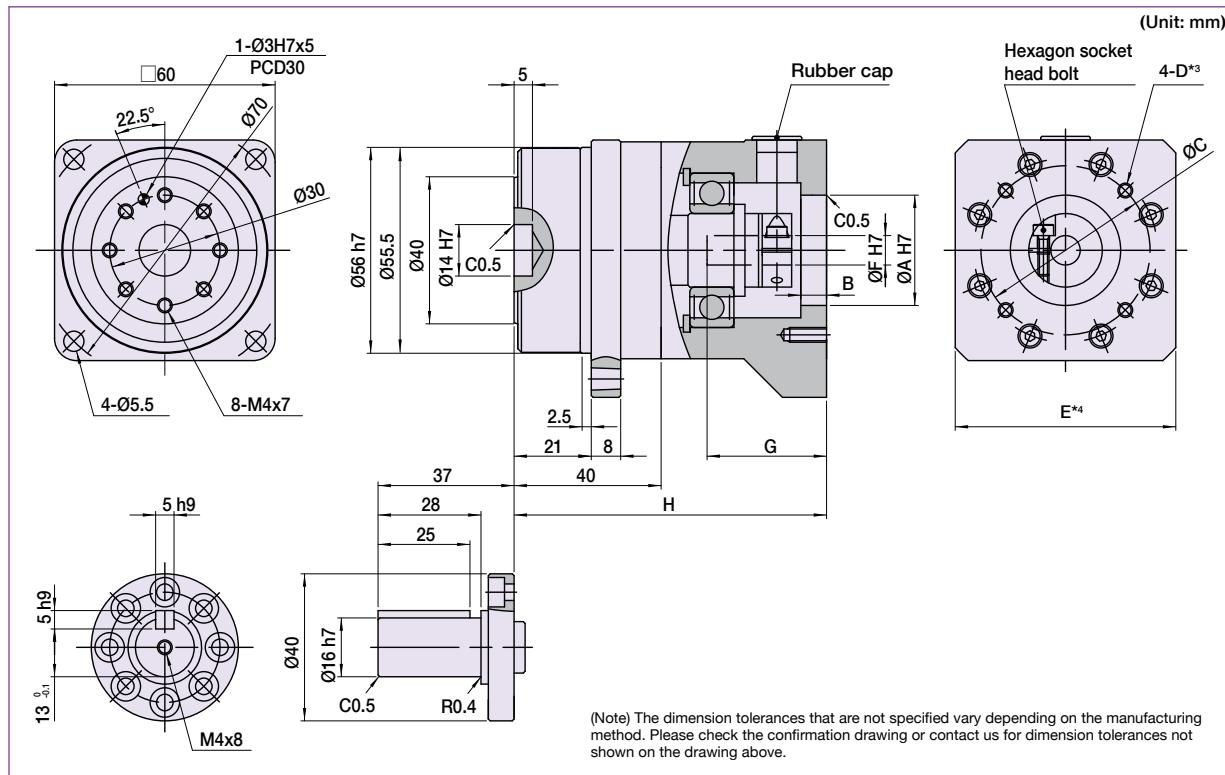
(10<sup>-4</sup> kgm<sup>2</sup>) Table 022-2

HPGP 11	Coupling	Ratio	5	21	37	45
		1	0.006	0.004	0.0027	0.0025

## HPGP-14 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

Figure 023-1



## Dimension Table

(Unit: mm) Table 023-1

Flange	Coupling	A (H7)		B	C		F (H7)		G		H *1	Mass (kg) *2	
		Min.	Max.		Max.	Min.	Max.	Min.	Max.	Min.	Max.	Shaft	Flange
Type I	1	30	58	7	35	74	6.0	7.8	21.5	32.5	85	1.07	0.95
Type II	1	40	70	7	45	84	9.0	14.2	25.8	33.8	85	1.12	1.00

Refer to the confirmation drawing for detailed dimensions. Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

\*4 E dimension is dependent on motor selection.

## Moment of Inertia

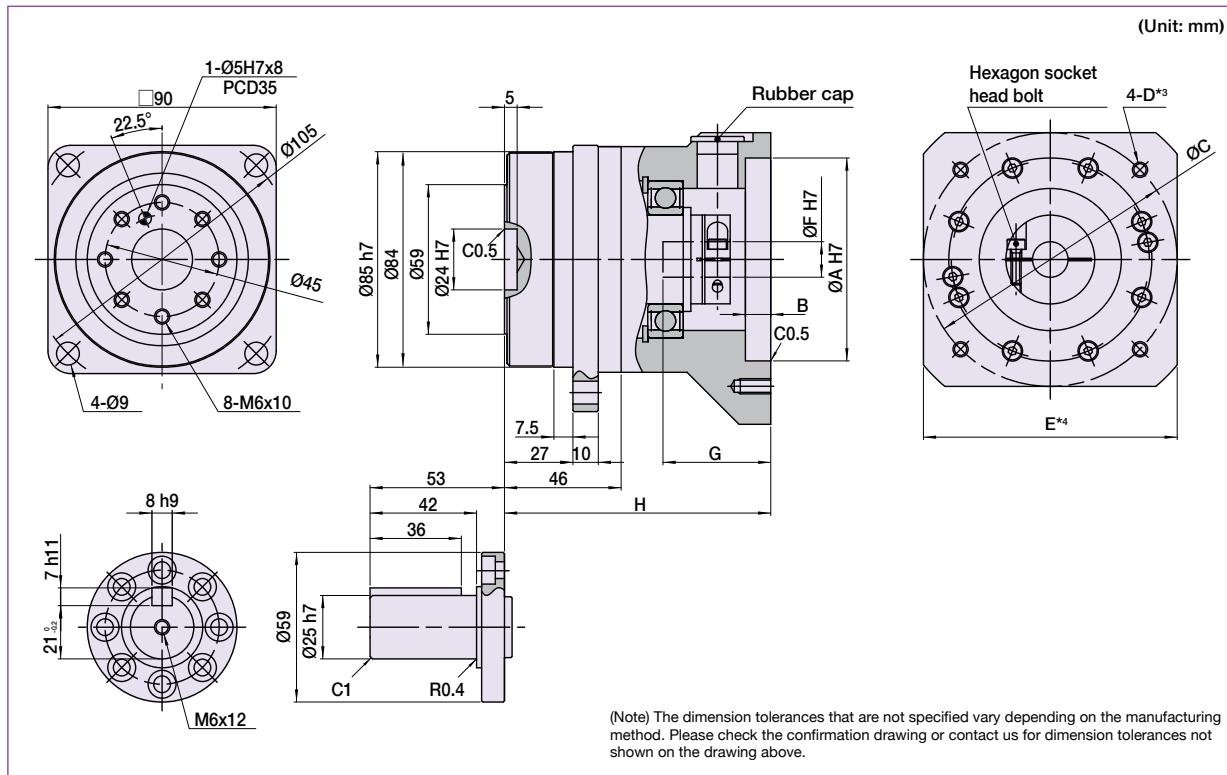
(10<sup>-4</sup> kgm<sup>2</sup>) Table 023-2

HPGP 14	Ratio Coupling	5	11	15	21	33	45
		-	0.06	0.058	0.05	0.044	0.044
	2	0.204	0.197	0.195	-	-	-

## HPGP-20 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

Figure 024-1



## Dimension Table

(Unit: mm) Table 024-1

Flange	Coupling	A (H7)		B	C		F (H7)		G		H *1	Mass (kg) *2		
		Min.	Max.		Min.	Max.	Min.	Max.	Min.	Max.		Typical	Shaft	
Type I	1	50	72	8	55	80	7.0	19.6	23.0	35.5	98.0	3.1	2.7	
Type II	1	80	98	10	90	120	7.0	19.6	30.0	42.5	105.0	3.3	2.9	
Type III	3	30	45	10	35	50	7.0	7.8	21.0	31.0	93.5	2.6	2.2	
Type IV	1	46	70	10	55	96	7.0	19.6	30.0	42.5	105.0	3.3	2.9	
-33 Ratio	Type I	1	50	72	8	55	80	7.0	19.6	23.0	35.5	103.0	3.1	2.7
	Type II	1	80	98	10	90	120	7.0	19.6	30.0	42.5	110.0	3.3	2.9
	Type III	3	30	45	10	35	50	7.0	7.8	21.0	31.0	98.5	2.6	2.2
	Type IV	1	46	70	10	55	96	7.0	19.6	30.0	42.5	103.0	3.3	2.9

Refer to the confirmation drawing for detailed dimensions. Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

\*4 E dimension is dependent on motor selection.

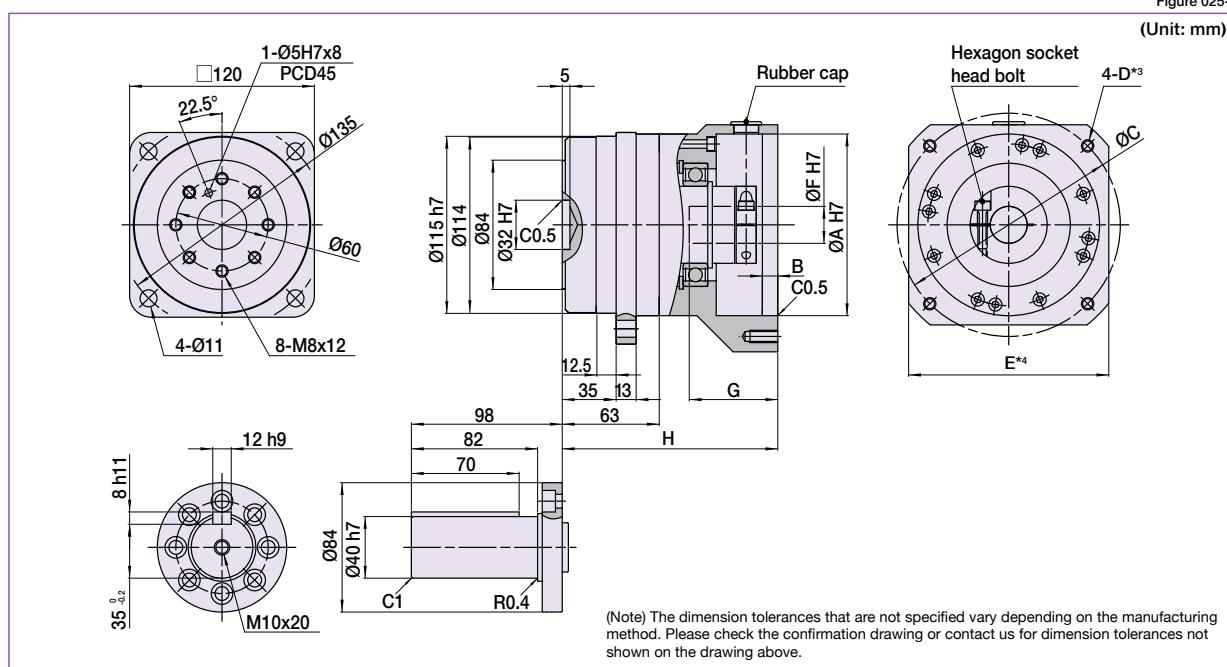
## Moment of Inertia

(10<sup>-4</sup> kgm<sup>2</sup>) Table 024-2

HPGP 20	Ratio Coupling	5	11	15	21	33	45
		1	0.69	0.62	0.58	0.5	0.45
	2	-	-	-	0.12	0.071	0.063

## HPGP-32 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.



## Dimension Table

(Unit: mm) Table 025-1

Flange	Coupling	A (H7)		B		C		F (H7)		G		H *1	Mass (kg) *2	
		Min.	Max.	Max.	Min.	Max.	Min.	Max.	Min.	Max.	Typical	Shaft	Flange	
Type I	1	110	120	10	120	155	10.0	28.6	31.0	57.5	140	3.1	2.7	
Type II	1	70	100	7	80	112	10.0	28.6	30.0	56.5	139	3.3	2.9	
Type III	3	50	100	10	80	112	14.0	19.6	25.8	38.8	139	2.6	2.2	
Type IV	1	70	95	10	80	115	10.0	28.6	41.0	67.5	150	3.3	2.9	
Type V	1	70	110	10	80	155	10.0	28.6	45.0	71.5	154	3.3	2.9	
-33 Ratio	Type I	110	120	10	120	155	10.0	28.6	31.0	57.5	145	3.1	2.7	
	Type II	70	100	7	80	112	10.0	28.6	30.0	56.5	144	3.3	2.9	
	Type III	50	100	10	80	112	14.0	19.6	25.8	38.8	144	2.6	2.2	
	Type IV	70	95	10	80	115	10.0	28.6	41.0	67.5	155	3.3	2.9	
	Type V	70	110	10	80	155	10.0	28.6	45.0	71.5	159	3.3	2.9	

Refer to the confirmation drawing for detailed dimensions. Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

\*4 E dimension is dependent on motor selection.

## Moment of Inertia

(10<sup>-4</sup> kgm<sup>2</sup>) Table 025-2

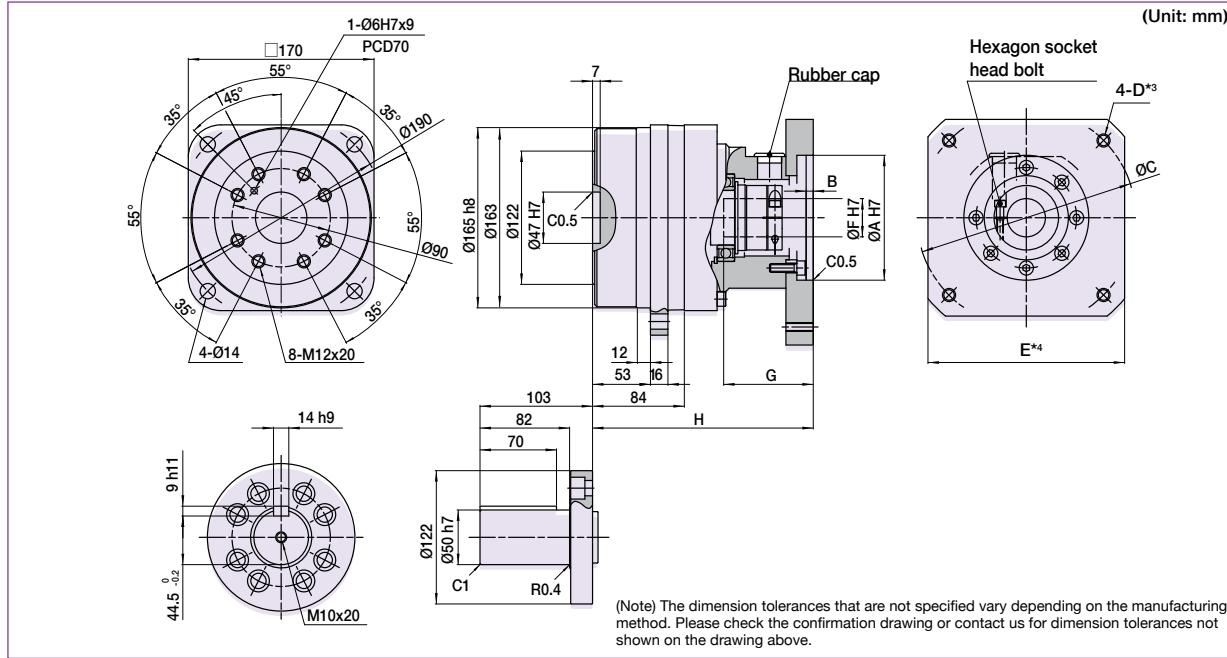
HPGP 32	Ratio	5	11	15	21	33	45
	Coupling	3.9	3.7	3.5	3	2.8	.8
	1	3.9	3.7	3.5	3	2.8	.8
2	-	-	-	0.84	0.66	0.61	

## HPGP-50 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

Figure 026-1

(Unit: mm)



(Note) The dimension tolerances that are not specified vary depending on the manufacturing method. Please check the confirmation drawing or contact us for dimension tolerances not shown on the drawing above.

## Dimension Table

(Unit: mm) Table 026-1

Flange	Coupling	A (H7)		B	C		F (H7)		G		H *1	Mass (kg) *2	
		Min.	Max.		Max.	Min.	Max.	Min.	Max.	Min.	Max.	Typical	Shaft
Type I	1	70	200	15	90	235	19.0	41.0	45.0	81.0	202	20.2	17.2
Type II	1	70	200	15	90	235	19.0	41.0	45.0	81.0	243.5	20.4	17.4
Type III	2	80	115	10	100	150	19.0	41.0	31.5	55.0	176	19.0	16.0
Type IV	1	70	200	15	90	235	19.0	41.0	45.0	81.0	202	27.5	24.5

Refer to the confirmation drawing for detailed dimensions. Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

\*4 E dimension for Flange Type I, II, and IV is dependent on motor selection.

## Moment of Inertia

(10<sup>-4</sup> kgm<sup>2</sup>) Table 026-2

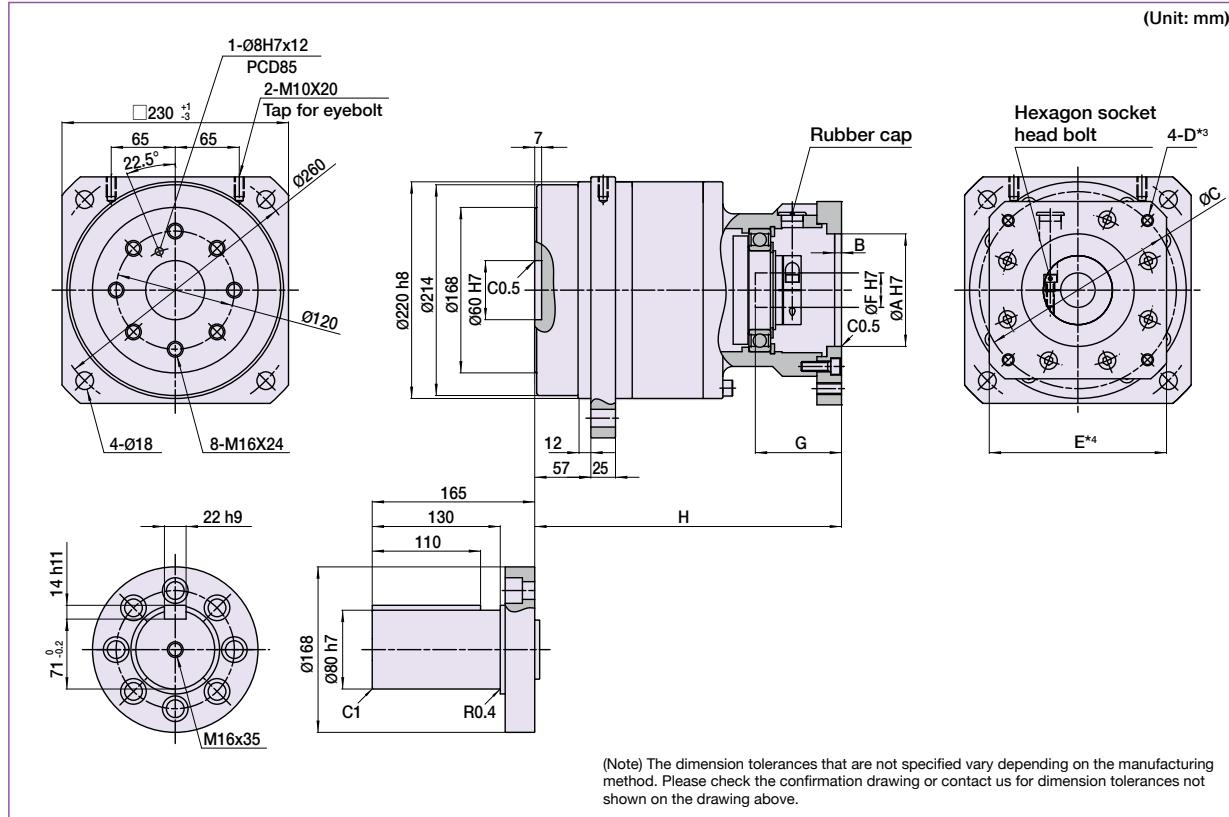
HPGP 50	Ratio Coupling	5	11	15	21	33	45
		1	12	9.4	9.1	7	6.1
	2	-	-	8.3	5.8	4.9	4.7

## HPGP-65 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

Figure 027-1

(Unit: mm)



## Dimension Table

(Unit: mm) Table 027-1

	Flange	Coupling	A (H7)		B	C		F (H7)		G		H *1	Mass (kg) *2	
			Min.	Max.		Min.	Max.	Min.	Max.	Min.	Max.	Typical	Shaft	Flange
Single Stage	Type I	1	125	230	15	150	265	35.0	43.9	63.0	87.5	241.5	48.0	38.0
Two Stage	Type I	1	125	230	15	150	265	35.0	43.9	63.0	87.5	311.5	52.0	42.0

Refer to the confirmation drawing for detailed dimensions. Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

\*4 E dimension is dependent on motor selection.

## Moment of Inertia

(10<sup>-4</sup> kgm<sup>2</sup>) Table 027-2

HPGP 65	Ratio							
		4	5	12	15	20	25	
	Coupling	1	-	-	28	27	15	15
	2	92	-	77	69	57	56	

## Product Sizing & Selection

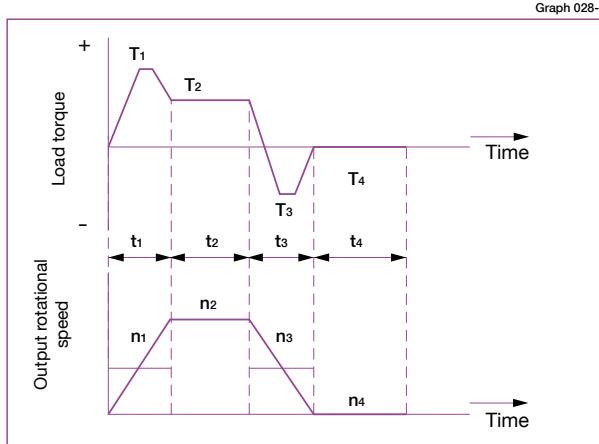
To fully utilize the excellent performance of the HPGP HarmonicPlanetary® gearheads, check your operating conditions and, using the flowchart, select the appropriate size gear for your application.

In general, a servo system rarely operates at a continuous load and speed. The input speed, load torque change and a comparatively large torque is applied during start and stop. Unexpected impact torques may also be applied.

Check your operating conditions against the following load torque pattern and select a suitable size based on the flowchart shown on the right. Also check the life and static safety coefficient of the cross roller bearing and input side main bearing (input shaft type only).

### Checking the load torque pattern

Review the load torque pattern. Check the specifications shown in the figure below.



#### Obtain the value of each load torque pattern.

Load torque	T <sub>1</sub> to T <sub>n</sub> (Nm)
Time	t <sub>1</sub> to t <sub>n</sub> (sec)
Output rotational speed	n <sub>1</sub> to n <sub>n</sub> (rpm)

#### <Normal operation pattern>

Starting	T <sub>1</sub> , t <sub>1</sub> , n <sub>1</sub>
Steady operation	T <sub>2</sub> , t <sub>2</sub> , n <sub>2</sub>
Stopping (slowing)	T <sub>3</sub> , t <sub>3</sub> , n <sub>3</sub>
Idle	T <sub>4</sub> , t <sub>4</sub> , n <sub>4</sub>

#### <Maximum rotational speed>

Max. output rotational speed	no max ≥ n <sub>1</sub> to n <sub>n</sub>
Max. input rotational speed	n <sub>i max</sub> n <sub>1</sub> × R to n <sub>n</sub> × R
(Restricted by motors)	R: Reduction ratio

#### <Impact torque>

When impact torque is applied T<sub>s</sub>

#### <Required life>

L<sub>50</sub> = L (hours)

### Flowchart for selecting a size

Please use the flowchart shown below for selecting a size. Operating conditions must not exceed the performance ratings.

Calculate the average load torque applied on the output side from the load torque pattern: T<sub>av</sub> (Nm).

$$T_{av} = \frac{1^{0.3} (n_1 \cdot t_1 \cdot |T_1|)^{0.3} + n_2 \cdot t_2 \cdot |T_2|^{0.3} + \dots + n_n \cdot t_n \cdot |T_n|^{0.3}}{n_1 \cdot t_1 + n_2 \cdot t_2 + \dots + n_n \cdot t_n}$$

Calculate the average output speed based on the load torque pattern: no av (rpm)

$$no\ av = \frac{|n_1| \cdot t_1 + |n_2| \cdot t_2 + \dots + |n_n| \cdot t_n}{t_1 + t_2 + \dots + t_n}$$

Make a preliminary model selection with the following condition: T<sub>av</sub> ≤ Average load torque (Refer to rating table).



Determine the reduction ratio (R) based on the maximum output rotational speed (no max) and maximum input rotational speed (n<sub>i max</sub>).

$$\frac{n_{i\ max}}{no\ max} \geq R$$

(A limit is placed on n<sub>i max</sub> by motors.) Calculate the maximum input speed (n<sub>i max</sub>) from the maximum output speed (no max) and the reduction ratio (R). n<sub>i max</sub>=no max × R



Calculate the average input speed (n<sub>av</sub>) from the average output speed (no av) and the reduction ratio (R): n<sub>i av</sub> = no av · R ≤ Max. average input speed (nr).



Check whether the maximum input speed is equal to or less than the values in the rating table.  
n<sub>i max</sub> ≤ maximum input speed (rpm)



Check whether T<sub>1</sub> and T<sub>3</sub> are within peak torques (Nm) on start and stop in the rating table.



Check whether T<sub>s</sub> is equal to or less than the momentary max. torque (Nm) value from the ratings.



Calculate the lifetime and check whether it meets the specification requirement.

$$Tr: Output torque  
Nr: Max. average input speed  
L<sub>10</sub>=20,000 \cdot \left( \frac{T_r}{T_{av}} \right)^{10/3} \cdot \left( \frac{n_r}{n_{i\ av}} \right) \text{ (Hour)}$$



The model number is confirmed.

Review the operation conditions, size and reduction ratio.

Refer to the Caution note below.

#### Caution

If the expected operation will result in conditions where:  
i) Actual average load torque (T<sub>av</sub>) > Permissible maximum value of average load torque or  
ii) Actual average input rotational speed (n<sub>i av</sub>) > Permissible average input rotational speed (nr), then please check its effect on the speed reducer temperature rise or other factors. Consider selecting the next larger speed reducer, change the operating loads or take other means to ensure safe use of the gear. Exercise caution especially when the duty cycle is close to continuous operation.

## Example of model number Selection

## Value of each load torque pattern.

Load torque  $T_n$  (Nm)  
 Time  $t_n$  (sec)  
 Output rotational speed  $n_n$  (rpm)

## &lt;Normal operation pattern&gt;

Starting  $T_1 = 70 \text{ Nm}$ ,  $t_1 = 0.3 \text{ sec}$ ,  $n_1 = 60 \text{ rpm}$   
 Steady operation  $T_2 = 18 \text{ Nm}$ ,  $t_2 = 3 \text{ sec}$ ,  $n_2 = 120 \text{ rpm}$   
 Stopping (slowing)  $T_3 = 35 \text{ Nm}$ ,  $t_3 = 0.4 \text{ sec}$ ,  $n_3 = 60 \text{ rpm}$   
 Idle  $T_4 = 0 \text{ Nm}$ ,  $t_4 = 5 \text{ sec}$ ,  $n_4 = 0 \text{ rpm}$

<Maximum rotational speed>  
 Max. output rotational speed  $n_{max} = 120 \text{ rpm}$   
 Max. input rotational speed  $n_{i max} = 5,000 \text{ rpm}$   
 (Restricted by motors)

<Impact torque>  
 When impact torque is applied  $T_s = 180 \text{ Nm}$

<Required life>  
 $L_{50} = 30,000 \text{ (hours)}$

Calculate the average load torque applied to the output side based on the load torque pattern:  $T_{av}$  (Nm).

$$T_{av} = \sqrt[10/3]{\frac{|60\text{rpm}| \cdot 0.3\text{sec} \cdot |70\text{Nm}|^{10/3} + |120\text{rpm}| \cdot 3\text{sec} \cdot |18\text{Nm}|^{10/3} + |60\text{rpm}| \cdot 0.4\text{sec} \cdot |35\text{Nm}|^{10/3}}{|60\text{rpm}| \cdot 0.3\text{sec} + 120\text{rpm} \cdot 3\text{sec} + |60\text{rpm}| \cdot 0.4\text{sec}|}}$$

Calculate the average output speed based on the load torque pattern: no  $av$  (rpm)

$$\text{no } av = \frac{|60\text{rpm}| \cdot 0.3\text{sec} + |120\text{rpm}| \cdot 3\text{sec} + |60\text{rpm}| \cdot 0.4\text{sec} + |0\text{rpm}| \cdot 5\text{sec}}{0.3\text{sec} + 3\text{sec} + 0.4\text{sec} + 5\text{sec}}$$

Refer to the Caution note at the bottom of page 28.

Make a preliminary model selection with the following conditions.  $T_{av} = 30.2 \text{ Nm} \leq 72 \text{ Nm}$ . (HPGP-20A-33 is tentatively selected based on the average load torque (see the rating table) of size 20 and reduction ratio of 33.)



Determine a reduction ratio ( $R$ ) from the maximum output speed (no  $max$ ) and maximum input speed ( $n_{i max}$ ).

$$\frac{5,000 \text{ rpm}}{120 \text{ rpm}} = 41.7 \geq 33$$

Calculate the maximum input speed ( $n_{i max}$ ) from the maximum output speed (no  $max$ ) and reduction ratio ( $R$ ):  $n_{i max} = 120 \text{ rpm} \cdot 33 = 3,960 \text{ rpm}$



Calculate the average input speed ( $ni_{av}$ ) from the average output speed (no  $av$ ) and reduction ratio ( $R$ ):  
 $ni_{av} = 46.2 \text{ rpm} \cdot 33 = 1,525 \text{ rpm} \leq \text{Max average input speed of size 20 } 3,000 \text{ rpm}$



Check whether the maximum input speed is equal to or less than the values specified in the rating table.  
 $n_{i max} = 3,960 \text{ rpm} \leq 5,000 \text{ rpm}$  (maximum input speed of size 20)



Check whether  $T_1$  and  $T_3$  are within peak torques (Nm) on start and stop in the rating table.  
 $T_1 = 70 \text{ Nm} \leq 156 \text{ Nm}$  (Limit for repeated peak torque, size 20)  
 $T_3 = 35 \text{ Nm} \leq 156 \text{ Nm}$  (Limit for repeated peak torque, size 20)



Check whether  $T_s$  is equal to or less than limit for momentary torque (Nm) in the rating table.  
 $T_s = 180 \text{ Nm} \leq 217 \text{ Nm}$  (momentary max. torque of size 20)



Calculate life and check whether the calculated life meets the requirement.

$$L_{50} = 20,000 \cdot \left( \frac{72 \text{ Nm}}{30.2 \text{ Nm}} \right)^{10/3} \cdot \left( \frac{3,000 \text{ rpm}}{1,525 \text{ rpm}} \right) = 712,251 \text{ (hours)} \geq 30,000 \text{ (hours)}$$



The selection of model number HPGP-20A-33 is confirmed from the above calculations.

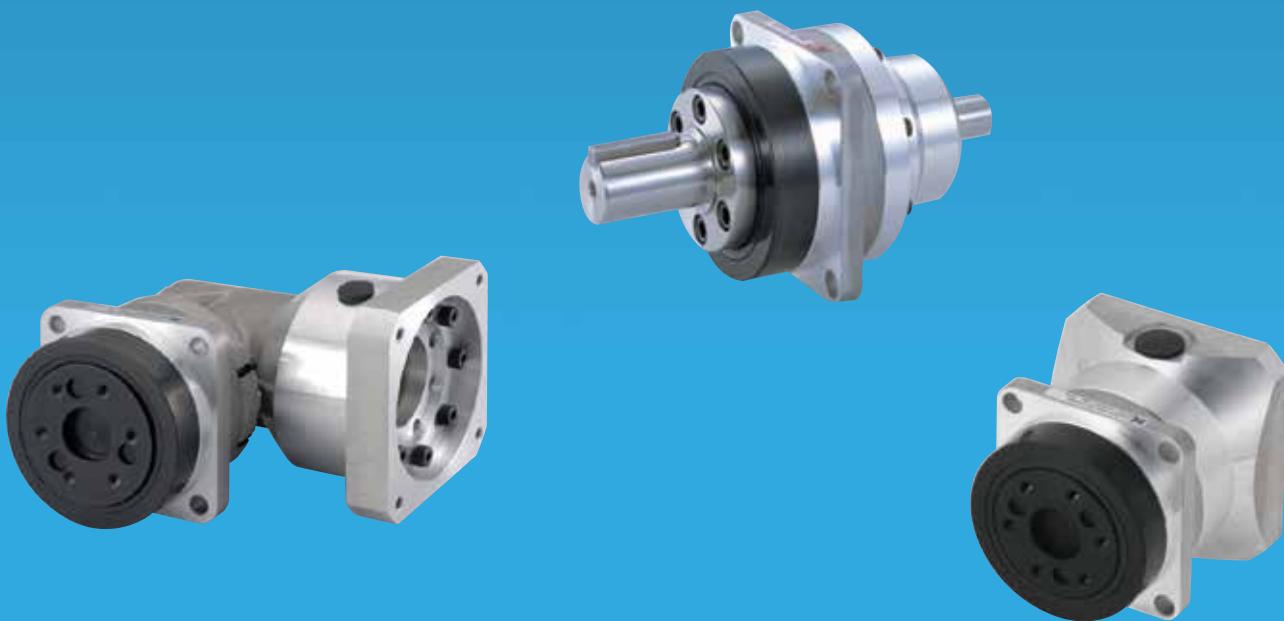
Review the operation conditions, size and reduction ratio.

# HarmonicPlanetary® HPGP / HPG Series

The thin wall flexible gear technology used for HarmonicDrive® gearing is applied to the internal gear of our planetary gear speed reducers. It allows the internal gear to deform elastically thus maintaining low backlash for the life of the gearhead, without the need for adjustment.

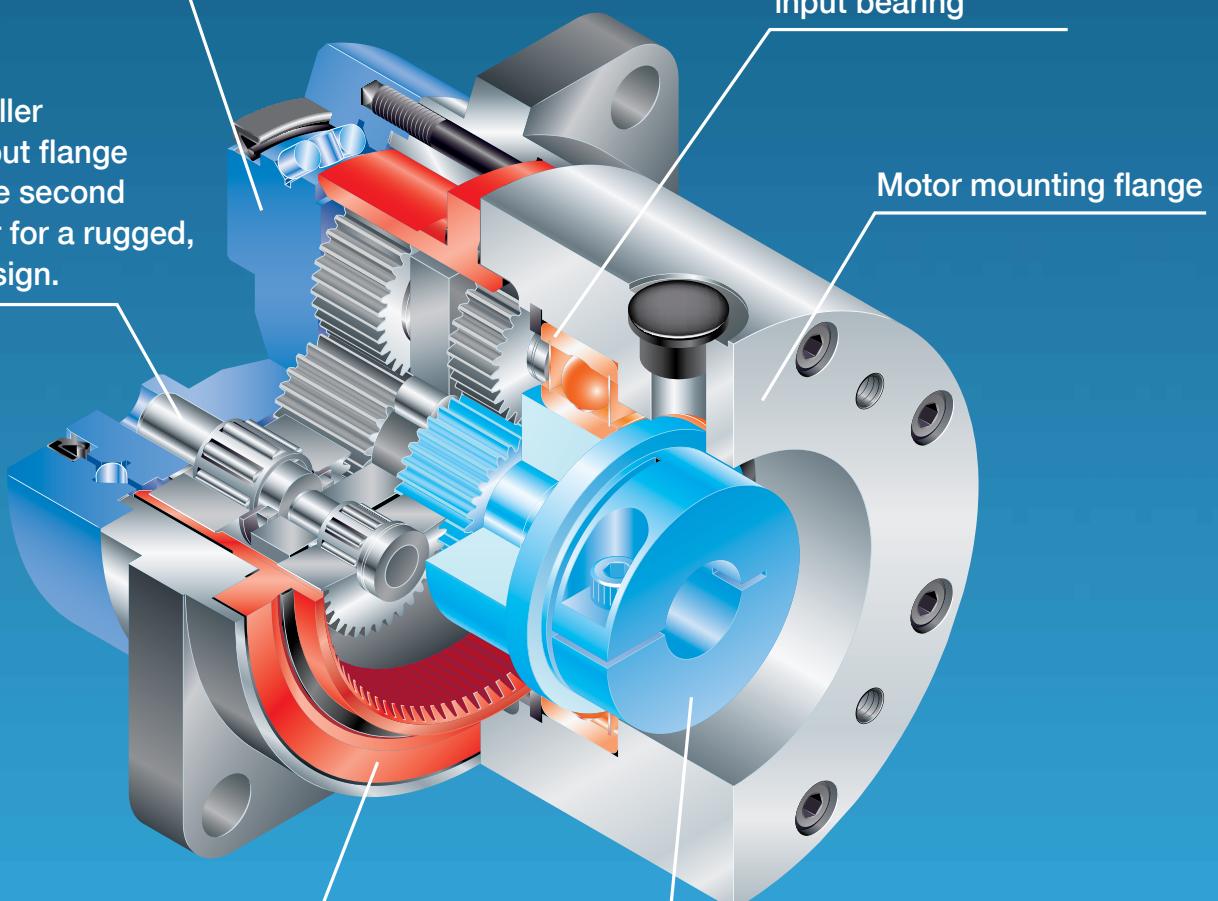
Planetary gears have simultaneous meshing between the sun gear and planet gears and between the planet gears and the internal gear. Some manufacturers try to reduce the backlash by controlling the dimensional precision of the parts, however this causes interference of meshing parts due to dimensional errors, resulting in uneven input torque and noise. Harmonic Planetary gears use a thin wall elastic internal gear which allows a preload of the gear and compensates for interference between meshing parts. The Harmonic Planetary® gear series incorporates this internal gear which maintains low backlash for the life of the speed reducer.

- ◆ **Low backlash: Less than 3 arc-min (Less than 1 arc-min also available)**
- ◆ **Low gear ratios, 3:1 to 50:1**
- ◆ **High efficiency**
- ◆ **High load capacity by integrating structure with cross roller bearing**
- ◆ **High-torque capacity**



**Robust cross roller bearing and output flange are integrated to provide high moment stiffness, high load capacity and precise positioning accuracy.**

The cross roller bearing output flange serves as the second stage carrier for a rugged, compact design.



**Quick Connect™ coupling for easy mounting of any servomotor**

## Output Bearing Specifications and Checking Procedure

A precision cross roller bearing supports the external load (output flange).

Check the maximum load, moment load, life of the bearing and static safety coefficient to maximize performance.

### Checking procedure

#### (1) Checking the maximum load moment load ( $M_{max}$ )

Obtain the maximum load moment load ( $M_{max}$ ).  Maximum load moment load ( $M_{max}$ )  $\leq$  Permissible moment ( $M_c$ )

#### (2) Checking the life

Obtain the average radial load ( $F_{avr}$ ) and the average axial load ( $F_{axr}$ ).  Obtain the radial load coefficient ( $X$ ) and the axial load coefficient ( $Y$ ).  Calculate the life and check it.

#### (3) Checking the static safety coefficient

Obtain the static equivalent radial load coefficient ( $P_o$ ).  Check the static safety coefficient. ( $f_s$ )

### Specification of output bearing

**HPGP/HPG Series** Table 129-1, -2 and -3 indicate the specifications for gearbox, right angle and input shaft unit, and cross roller bearing.

Table 129-1

Size	Pitch circle	Offset amount	Basic rated load			Allowable moment load $M_c^{*3}$		Moment stiffness $Km^{*4}$		
	dp	R	Basic dynamic load rating $C^{*1}$		Basic static load rating $C_0^{*2}$	Nm	Kgfm	$\times 10^4$ Nm/rad	Kgfm/arc min	
	m	m	N	kgf	N	kgf	Nm	Kgfm	$\times 10^4$ Nm/rad	Kgfm/arc min
11	0.0275	0.006	3116	318	4087	417	9.50	0.97	0.88	0.26
14	0.0405	0.011	5110	521	7060	720	32.3	3.30	3.0	0.90
20	0.064	0.0115	10600	1082	17300	1765	183	18.7	16.8	5.0
32	0.085	0.014	20500	2092	32800	3347	452	46.1	42.1	12.5
50	0.123	0.019	41600	4245	76000	7755	1076	110	100	29.7
65	0.170	0.023	90600	9245	148000	15102	3900	398	364	108

Table 129-2

Size	Reduction ratio	Allowable radial load <sup>*5</sup>		Allowable axial load <sup>*5</sup>	
		N	N	N	N
11	5	280		430	
	(9)	340		510	
	21	440		660	
	37	520		780	
	45	550		830	
14	(3)	400		600	
	5	470		700	
	11	600		890	
	15	650		980	
	21	720		1080	
	33	830		1240	
	45	910		1360	
20	(3)	840		1250	
	5	980		1460	
	11	1240		1850	
	15	1360		2030	
	21	1510		2250	
	33	1729		2580	
	45	1890		2830	

\* The ratio specified in parentheses is for the HPG Series.

Table 129-3

Size	Reduction ratio	Allowable radial load <sup>*5</sup>		Allowable axial load <sup>*5</sup>	
		N	N	N	N
32	(3)	1630		2430	
	5	1900		2830	
	11	2410		3590	
	15	2640		3940	
	21	2920		4360	
	33	3340		4990	
50	45	3670		5480	
	(3)	3700		5570	
	5	4350		6490	
	11	5500		8220	
	15	6050		9030	
	21	6690		9980	
	33	7660		11400	
65	45	8400		12500	
	4	8860		13200	
	5	9470		14100	
	12	12300		18300	
	15	13100		19600	
	20	14300		21400	
	25	15300		22900	
	(40)	17600		26300	
	(50)	18900		28200	

\* The ratio specified in parentheses is for the HPG Series.

\*1 The basic dynamic load rating means a certain static radial load so that the basic dynamic rated life of the roller bearing is a million rotations.

\*2 The basic static load rating means a static load that gives a certain level of contact stress ( $4kN/mm^2$ ) in the center of the contact area between rolling element receiving the maximum load and orbit.

\*3 The allowable moment load is a maximum moment load applied to the bearing. Within the allowable range, basic performance is maintained and the bearing is operable. Check the bearing life based on the calculations shown on the next page.

\*4 The value of the moment stiffness is the average value.

\*5 The allowable radial load and allowable axial load are the values that satisfy the life of a speed reducer when a pure radial load or an axial load applies to the main bearing. ( $L_r + R = 0 \text{ mm}$  for radial load and  $L_a = 0 \text{ mm}$  for axial load) If a compound load applies, refer to the calculations shown on the next page.

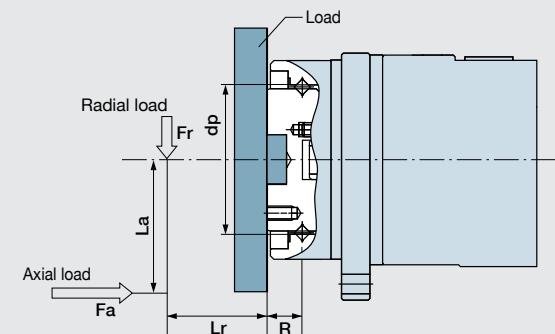
Figure 131-1

## How to calculate the maximum load moment load

HPGP HPG CSG-GH  
CSF-GH HPF

Maximum load moment load ( $M_{max}$ ) is obtained as follows.  
Make sure that  $M_{max} \leq M_c$ .

Formula 131-1			
$M_{max} = F_{r\ max}(L_r + R) + F_{a\ max} L_a$			
$F_{r\ max}$	Max. radial load	N (kgf)	See Fig. 131-1.
$F_{a\ max}$	Max. axial load	N (kgf)	See Fig. 131-1.
$L_r, L_a$	—	m	See Fig. 131-1.
R	Offset amount	m	See Fig. 131-1. See "Specification of main bearing" of each series



## How to calculate the radial load coefficient and the axial load coefficient

HPGP HPG CSG-GH  
CSF-GH HPF

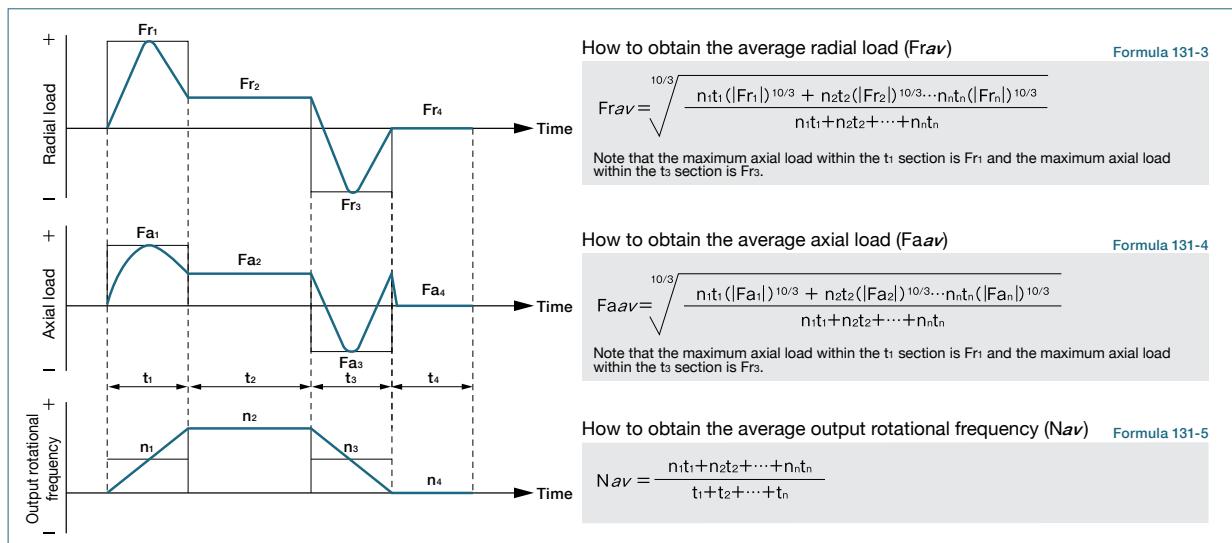
The radial load coefficient (X) and the axial load coefficient (Y)

Formula		X	Y
$F_{rav}$	$\frac{F_{rav} + 2(F_{rav}(L_r + R) + F_{aav} \cdot L_a)}{dp}$	1	0.45
$F_{aav}$	$\frac{F_{aav} + 2(F_{rav}(L_r + R) + F_{aav} \cdot L_a)}{dp}$	0.67	0.67
$F_{rav}$	Average radial load	N (kgf)	See "How to obtain the average load."
$F_{aav}$	Average axial load	N (kgf)	See "How to obtain the average load."
$L_r, L_a$	—	m	See Fig. 131-1.
R	Offset amount	m	See Fig. 131-1. See "Output Shaft Bearing Specifications" of each series.
dp	Circular pitch of roller	m	See Fig. 131-1. See "Output Shaft Bearing Specifications" of each series.

## How to calculate the average load (Average radial load, average axial load, average output rotational frequency)

HPGP HPG CSG-GH CSF-GH HPF

If the radial load and the axial load fluctuate, they should be converted into the average load to check the life of the cross roller bearing.



## How to calculate the life

HPGP

HPG

CSG-GH

CSF-GH

HPF

Calculate the life of the cross roller bearing using Formula 132-1. You can obtain the dynamic equivalent radial load (Pc) using Formula 132-2.

Formula 132-1

$$L_{10} = \frac{10^6}{60 \times N_{av}} \times \left( \frac{C}{f_w \cdot P_c} \right)^{10/3}$$

<b>L<sub>10</sub></b>	Life	hour	—
<b>N<sub>av</sub></b>	Ave. output speed	rpm	See "How to calculate the ave. load."
<b>C</b>	Basic dynamic rated load	N (kgf)	See "Output Bearing Specs."
<b>P<sub>c</sub></b>	Dynamic equi. radial load	N (kgf)	See Formula 132-2.
<b>f<sub>w</sub></b>	Load coefficient	—	See Table 132-1.

Formula 132-2

$$P_c = X \cdot \left( F_{rav} + \frac{2(F_{rav}(L_r + R) + F_{aav} \cdot L_a)}{dp} \right) + Y \cdot F_{aav}$$

<b>F<sub>rav</sub></b>	Average radial load	N (kgf)	See "How to calculate the ave. load."
<b>F<sub>aav</sub></b>	Average axial load	N (kgf)	See "Output Bearing Specs."
<b>dp</b>	Circular pitch of roller	m	See "Output Bearing Specs."
<b>X</b>	Radial load coefficient	—	See "How to calculate the radial load coefficient and the axial load coefficient."
<b>Y</b>	Axial load coefficient	—	See Figure 131-1. See "External load influence diagram."
<b>L<sub>r</sub>, L<sub>a</sub></b>	—	m	See Figure 131-1. See "External load influence diagram" and "Output Bearing Specs" of each series.
<b>R</b>	Offset amount	m	See Figure 131-1. See "External load influence diagram" and "Output Bearing Specs" of each series.

## Load coefficient

Table 132-1

Load status	f <sub>w</sub>
During smooth operation without impact or vibration	1 to 1.2
During normal operation	1.2 to 1.5
During operation with impact or vibration	1.5 to 3

## How to calculate the life during oscillating movement

HPGP

HPG

CSG-GH

CSF-GH

HPF

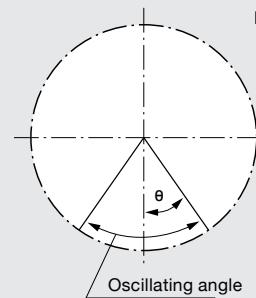
Calculate the life of the cross roller bearing during oscillating movement by Formula 132-3.

Figure 132-1

Formula 132-3

$$Loc = \frac{10^6}{60 \times n_1} \times \frac{90}{\theta} \times \left( \frac{C}{f_w \cdot P_c} \right)^{10/3}$$

<b>Loc</b>	Rated life under oscillating movement	hour	—
<b>n<sub>1</sub></b>	No. of reciprocating oscillation per min.	cpm	—
<b>C</b>	Basic dynamic rated load	N (kgf)	See "Output Bearing Specs."
<b>P<sub>c</sub></b>	Dynamic equivalent radial load	N (kgf)	See Formula 132-2.
<b>f<sub>w</sub></b>	Load coefficient	—	See Table 132-1.
<b>θ</b>	Oscillating angle /2	Deg.	See Figure 132-1.



Note: When the oscillating angle is small (5° or less), it is difficult to generate an oil film on the contact surface of the orbit ring, and the rolling element and fretting may be generated. Contact us if this happens.

**Note** When it is used for a long time while the rotation speed of the output shaft is in the ultra-low operation range (0.02rpm or less), the lubrication of the bearing becomes insufficient, resulting in deterioration of the bearing or increased load in the driving side. When using it in the ultra-low operation range, contact us.

## How to calculate the static safety coefficient

HPGP

HPG

CSG-GH

CSF-GH

HPF

In general, the basic static rated load (Co) is considered to be the permissible limit of the static equivalent load. However, obtain the limit based on the operating and required conditions. Calculate the static safety coefficient (fs) of the cross roller bearing using Formula 132-4.

General values under the operating condition are shown in Table 132-2. You can calculate the static equivalent radial load (Po) using Formula 132-5.

Formula 132-4

$$fs = \frac{Co}{Po}$$

<b>Co</b>	Basic static rated load	N (kgf)	See "Output Bearing Specs."
<b>Po</b>	Static equivalent radial load	N (kgf)	See Formula 132-5.

## Static safety coefficient

Table 132-2

Load status	fs
When high rotation precision is required	≥3
When impact or vibration is expected	≥2
Under normal operating condition	≥1.5

Formula 132-5

$$Po = Fr_{max} + \frac{2M_{max}}{dp} + 0.44Fa_{max}$$

<b>Fr<sub>max</sub></b>	Max. radial load	N (kgf)	See "How to calculate the max. load moment load."
<b>Fa<sub>max</sub></b>	Max. axial load	N (kgf)	See "Output Bearing Specs" of each series.
<b>M<sub>max</sub></b>	Max. load moment load	Nm (kgfm)	See "Output Bearing Specs" of each series.
<b>dp</b>	Circular pitch of roller	m	See "Output Bearing Specs" of each series.

## Input Bearing Specifications and Checking Procedure

Check the maximum load and life of the bearing on the input side if the reducer is an HPG input shaft unit or an HPF hollow shaft unit.

### Checking procedure

HPG

HPF

#### (1) Checking maximum load

Calculate:

Maximum load moment load ( $M_{i\ max}$ )  
Maximum load axial load ( $F_{ai\ max}$ )  
Maximum load radial load ( $F_{ri\ max}$ )



Maximum load moment load ( $M_{i\ max}$ )  $\leq$  Permissible moment load ( $M_c$ )  
Maximum load axial load ( $F_{ai\ max}$ )  $\leq$  Permissible axial load ( $F_{ac}$ )  
Maximum load radial load ( $F_{ri\ max}$ )  $\leq$  Permissible radial load ( $F_{rc}$ )

#### (2) Checking the life

Calculate:

Average moment load ( $M_{i\ av}$ )  
Average axial load ( $F_{ai\ av}$ )  
Average input speed ( $N_{i\ av}$ )



Calculate the life and check it.

## Specification of input shaft bearing

The specification of the input side main bearing of the input shaft unit is shown below.

### Specification of input shaft bearing

HPG

Table 133-1

Size	Basic rated load			
	Basic dynamic rated load $C_r$		Basic static rated load $C_{or}$	
	N	kgf	N	kgf
11	2700	275	1270	129
14	5800	590	3150	320
20	9700	990	5600	570
32	22500	2300	14800	1510
50	35500	3600	25100	2560
65	51000	5200	39500	4050

Table 133-2

Size	Allowable moment load $M_c$		Allowable axial load $F_{ac}^{*1}$		Allowable radial load $F_{rc}^{*2}$	
	Nm	kgfm	N	kgf	N	kgf
11	0.16	0.016	245	25	20.6	2.1
14	6.3	0.64	657	67	500	51
20	13.5	1.38	1206	123	902	92
32	44.4	4.53	3285	335	1970	201
50	96.9	9.88	5540	565	3226	329
65	210	21.4	8600	878	5267	537

### Specification of input shaft bearing

HPF

Table 133-3

Size	Basic rated load			
	Basic dynamic rated load $C_r$		Basic static rated load $C_{or}$	
	N	kgf	N	kgf
25	14500	1480	10100	1030
32	29700	3030	20100	2050

Table 133-4

Size	Allowable moment load $M_c$		Allowable axial load $F_{ac}^{*1}$		Allowable radial load $F_{rc}^{*3}$	
	Nm	kgfm	N	kgf	N	kgf
25	10	1.02	1538	157	522	53.2
32	19	1.93	3263	333	966	98.5

[Note: Table 133-2 and 133-4]

\*1 The allowable axial load is the tolerance of an axial load applied to the shaft center.

\*2 The allowable radial load of HPG series is the tolerance of a radial load applied to the shaft length center.

\*3 The allowable radial load of HPG series is the tolerance of a radial load applied to the point of 20 mm from the shaft edge (input flange edge).

## ■ Calculating maximum load moment load to input shaft

The maximum load moment load ( $M_{imax}$ ) is calculated as follows.  
Check that the following formulas are established in all circumstances:

Formula 134-1

$$M_{imax} = F_{ri\ max} \cdot L_{ri} + F_{ai\ max} \cdot L_{ai}$$

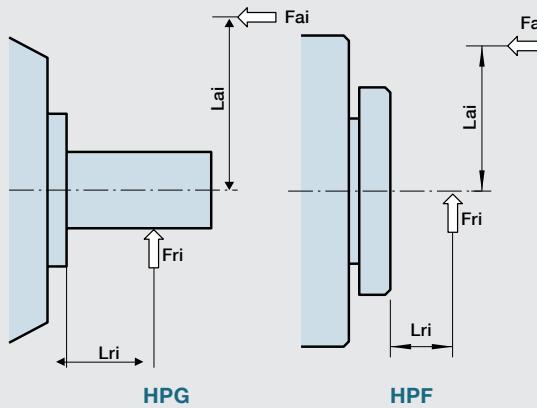
<b>Fri<sub>max</sub></b>	Max. radial load	N (kgf)	See Fig. 134-1.
<b>Fai<sub>max</sub></b>	Max. axial load	N (kgf)	See Fig. 134-1.
<b>L<sub>ri</sub>, L<sub>ai</sub></b>	— — —	m	See Fig. 134-1.

$M_{imax} \leq M_c$  (Permissible moment load)  
 $F_{ai\ max} \leq F_{ac}$  (Permissible axial load)

**HPG      HPF**

Figure 134-1

### External load influence diagram



## ■ How to calculate average load

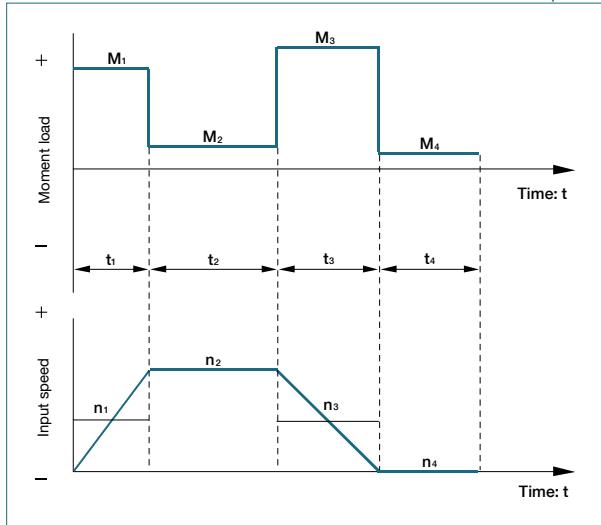
(Average moment load, average axial load, average input rotational frequency)

**HPG**

**HPF**

If moment load and axial load fluctuate, they should be converted into the average load to check the life of the bearing.

Graph 134-1



### How to calculate the average moment load (Miav)

Formula 134-2

$$Miav = \sqrt[3]{\frac{n_1 t_1 (|M_{i1}|)^3 + n_2 t_2 (|M_{i2}|)^3 + \dots + n_n t_n (|M_{in}|)^3}{n_1 t_1 + n_2 t_2 + \dots + n_n t_n}}$$

### How to calculate the average axial load (Faiav)

Formula 134-3

$$Faiav = \sqrt[3]{\frac{n_1 t_1 (|Fai_{i1}|)^3 + n_2 t_2 (|Fai_{i2}|)^3 + \dots + n_n t_n (|Fai_{in}|)^3}{n_1 t_1 + n_2 t_2 + \dots + n_n t_n}}$$

### How to calculate the average output rotational frequency (Niav)

Formula 134-4

$$Niav = \frac{n_1 t_1 + n_2 t_2 + \dots + n_n t_n}{t_1 + t_2 + \dots + t_n}$$

## ■ Calculating life of input side bearing

Calculate the bearing life according to Calculation Formula 132-5 and check the life.

Formula 134-5

$$L_{10} = \frac{10^6}{60 \times Niav} \times \left( \frac{Cr}{Pci} \right)^3$$

<b>L<sub>10</sub></b>	Life	Hour	—
<b>Niav</b>	Average input rotational speed	rpm	See Formula 134-4
<b>Cr</b>	Basic dynamic rated load	N (kgf)	See Table 133-1 and -3
<b>Pci</b>	Dynamic equivalent radial load	N	See Table 134-1 and -2

### Dynamic equivalent radial load

**HPG**

Table 134-1

Size	Pci
11	$0.444 \times Mi\ av + 1.426 \times Fai\ av$
14	$0.137 \times Mi\ av + 1.232 \times Fai\ av$
20	$0.109 \times Mi\ av + 1.232 \times Fai\ av$
32	$0.071 \times Mi\ av + 1.232 \times Fai\ av$
50	$0.053 \times Mi\ av + 1.232 \times Fai\ av$
65	$0.041 \times Mi\ av + 1.232 \times Fai\ av$

### Dynamic equivalent radial load

**HPF**

Table 134-2

Size	Pci
25	$121 \times Mi\ av + 2.7 \times Fai\ av$
32	$106 \times Mi\ av + 2.7 \times Fai\ av$

Miav Average moment load Nm (kgfm)

See Formula 134-2

Faiav Average axial load N (kgf)

See Formula 134-3

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